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Influence of hydrodynamic interactions on mechanical unfolding of proteins

P Szymczak¹ and Marek Cieplak²

 $^{\rm 1}$ Institute of Theoretical Physics, Warsaw University, ulica Hoża 69, 00-681 Warsaw, Poland

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Abstract

We incorporate hydrodynamic interactions in a structure-based model of ubiquitin and demonstrate that the hydrodynamic coupling may reduce the peak force when stretching the protein at constant speed, especially at larger speeds. Hydrodynamic interactions are also shown to facilitate unfolding at constant force and inhibit stretching by fluid flows.

(Some figures in this article are in colour only in the electronic version)

1. Introduction

It has been widely recognized that the water environment affects the energy landscape and functionality of biomolecules in a profound way. There is, however, another solvent-related effect that is considered less frequently: the hydrodynamic interactions (HI) between individual segments of a biomolecule that moves. These interactions may affect the dynamics of conformational changes because any motion of one segment generates a local fluid flow which influences another segment.

The presence of HI is known to affects dynamic properties of soft matter. For instance, HI modify the values of diffusion coefficients in colloidal suspensions [1], affect the characteristics of the coil-stretch transition in polymers [2], change the kinetic pathways of phase separation in binary mixtures [3], and alter the kinetics of macromolecule adsorption on surfaces [5]. Much less is known about the role of HI in protein folding and unfolding processes. Dickinson [4] and Tanaka [6] speculated that HI might affect the kinetics of protein folding, but the actual numerical assessment of the role of HI has come with the paper by Baumketner and Hiwatari [7]. They have considered coarse-grained models and found that HI delay folding of a β -hairpin but do not affect folding of the α -helix.

In this paper, we consider mechanical stretching of proteins and study the relevance of HI to the process. The stretching can be accomplished in several ways and we discuss three modes: at constant speed, at constant force, and through fluid flow. We chose ubiquitin as a model system, since there is a large body of experimental [8–11] and theoretical [12–17] data on its unfolding. A coarse-grained, Go-type model [18] of a protein is used, constructed based

² Institute of Physics, Polish Academy of Sciences, Aleja Lotników 32/46, 02-668 Warsaw, Poland

on the knowledge of its native state. The Go models have been shown to give surprisingly good agreement with both the experimental results [14, 19, 20] and all-atom molecular dynamic simulations [17] when it comes to stretching.

We outline the model in section 2, then introduce two different ways of tracking the evolution of the system: through Langevin dynamics and Brownian dynamics in sections 3 and 4 respectively. In the following sections we discuss results pertaining to the three modes of stretching and demonstrate that HI can take many roles: they inhibit unfolding by fluid flow, but make the constant-force stretching faster. At constant speed, they reduce the peak force if the speed is sufficiently high. This HI-related reduction in force may be downplayed in the all-atom simulations of titin by Lu and Schulten [21] which would provide a part explanation for the excessively large forces obtained in these studies.

2. The coarse-grained protein model

In our simulations, we use the coarse-grained, Go-type model of a protein. In the model, each residue is represented by a single bead centred on the position of the C^{α} atom. The successive beads along the backbone are tethered by harmonic potentials with a minimum at 3.8 Å. The other interactions between the residues are split into two classes: native and non-native. This determination is made by checking for native overlaps of all atoms in aminoacids when represented by enlarged van der Waals spheres as proposed in [22]. The aminoacids, i and j, that do overlap in this sense are endowed with the effective Lennard-Jones potential $V_{ij} = 4\epsilon \left[\left(\frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left(\frac{\sigma_{ij}}{r_{ij}} \right)^{6} \right]$. The length parameters σ_{ij} are chosen so that the potential minima correspond, pair by pair, to the experimentally established native distances between the respective amino-acids. In order to prevent emergence of entanglements, the non-native contacts are endowed with a hard-core repulsion described by the r_{ij}^{-12} part of the Lennard-Jones potential combined with a constant shift term that makes the potential vanish smoothly at 4 Å. The specificity of a protein is contained in the length parameters σ_{ij} . The energy parameter, ϵ , is taken to be uniform. We take $\epsilon/k_{\rm B}=900$ K, which correlates well with the data on titin and ubiquitin unfolding [14, 23]. Thus the reduced temperature, $\tilde{T} = k_{\rm B}T/\epsilon$, of 0.3 should be close to room temperature. All of the simulations reported here were performed at this temperature. Various simulation methods to study the dynamics of the system are outlined in the following sections.

3. Langevin dynamics (LD)

In this case, the dynamics of a protein is assumed to be governed by the Langevin equation

$$m\ddot{\mathbf{r}}_{i} = -\gamma \left(\dot{\mathbf{r}}_{i} - \mathbf{u}(\mathbf{r}_{i})\right) + \mathbf{F}_{i} + \Gamma_{i}. \tag{1}$$

Here, \mathbf{r}_i is the position of the *i*th amino-acid, \mathbf{F}_i is the net force on it due to intermolecular potentials, γ is the friction coefficient, and $\mathbf{u}(\mathbf{r}_i)$ denotes the solvent flow field. Finally, Γ is a white noise term with the dispersion obeying

$$\langle \mathbf{\Gamma}_i(t)\mathbf{\Gamma}_j(t')\rangle = 2k_{\rm B}T\gamma\delta(t-t')\mathbf{I}\delta_{ij}$$

where I is the identity matrix. The white noise term mimics the effect of the random collisions of the amino-acids with the surrounding solvent, at the same time serving as a thermostat of the system. However, this scheme completely neglects the effects of HI which may exist in a real system, when the motion of one particle induces the flow influencing the dynamics of all the other particles.

In the simulations, the friction coefficient γ is taken to be equal to $2m/\tau$ where $\tau = \sqrt{m\sigma^2/\epsilon} \approx 3$ ps is the characteristic timescale of oscillations in the Lennard-Jones well. The parameter $\sigma = 5$ Å used in the above definition is a characteristic value of σ_{ij} in the system. The selected value of γ corresponds to a situation in which the inertial effects are small [24, 25] but the damping action is not yet as strong as in water. The equations of motion are solved by a fifth-order predictor–corrector scheme.

Let us note, however, that although Langevin dynamics is commonly used in simulations of biological systems the validity of this approach is not always well established. Namely, as already noted by Lorentz [26], the Langevin equation in the above form may only be used if there is a separation of timescales between the relaxation time of the particle (i.e. the bead) velocity $\tau_v = \frac{m}{\gamma} = \frac{2a^2\rho}{9\eta}$ and the viscous relaxation time of the solvent, $\tau_{\eta} = a^2\frac{\rho_s}{\eta}$, where ρ is the density of the particle, a its radius, and ρ_s the density of the solvent (see also the thorough discussion in the book by Mazo [27]). The ratio of these two timescales is equal to $2\rho/9\rho_s$. Since the densities of proteins are only about 50% higher than those of the surrounding liquid [22], there is no strong separation of timescales between the relaxation of fluid variables and those of the bead and, strictly speaking, instead of equation (1) one should use the generalized Langevin equation involving a memory kernel

$$m\ddot{\mathbf{r}}_{i}(t) = -\int_{0}^{t} dt' \, \xi(t - t') (\dot{\mathbf{r}}_{i}(t') - \mathbf{u}(\mathbf{r}_{i}, t')) + \mathbf{F}_{i}(t) + \Gamma_{i}(t)$$
 (2)

where the noise is again Gaussian and related to the dissipative term through the generalized fluctuation—dissipation relation

$$\langle \mathbf{\Gamma}_i(t)\mathbf{\Gamma}_j(t')\rangle = k_{\rm B}T\xi(t-t')\mathbf{I}\delta_{ij}.$$

Such an approach is naturally much harder to implement (see, however, [28]) and thus the ordinary Langevin description as in equation (1) is usually resorted to. In this paper, we show that in protein unfolding simulations the results of a simple Langevin dynamics (1) are consistent with those of Brownian dynamics (see section 4). The latter is not affected by the solvent and particle inertia effects, hence the agreement between the two methods seems to imply that non-instantaneous response of the solvent to the change of particle velocity does not play any important role in the protein unfolding processes.

4. Brownian dynamics (BD)

If the momentum relaxation timescale (τ_v) is small in comparison to the timescales characterizing the conformational evolution of the system (τ_c) , it is appropriate to describe the dynamics in terms of equilibration of the particle configurations only. The exact definition of τ_c is problem dependent: if the protein is stretched by the flow U then $\tau_c = \frac{a}{U}$, if a force F acts on the molecule then $\tau_c = \frac{a\gamma}{F}$, and if the Brownian diffusion plays the central role in particle evolution then $\tau_c = a^2/D$ (where D is the diffusion constant and a the radius of the bead). The algorithm for simulations of the evolution of particle positions in this time regime has been devised by Ermak and McCammon [29]. The displacement of particle i in time step Δt (in the absence of the flow) obeys

$$\mathbf{r}_{i} - \mathbf{r}_{i}^{0} = \sum_{j} (\nabla_{j} \cdot \mathbf{D}_{ij}^{0}) \Delta t + \frac{1}{k_{\mathrm{B}}T} \sum_{j} \mathbf{D}_{ij}^{0} \cdot \mathbf{F}_{j}^{0} \Delta t + \mathbf{B}_{i},$$
(3)

where the index 0 denotes the values of respective quantities at the beginning of the time step, **D** is the diffusion tensor and **B** a random displacement given by a Gaussian distribution with

an average value of zero and covariance obeying

$$\langle \mathbf{B}_i \mathbf{B}_j \rangle = 2 \mathbf{D}_{ij}^0 \Delta t. \tag{4}$$

It is nontrivial to generalize the above expression to incorporate the effects of a general external flow field [30]. However, in the present case, we will be interested only in the uniform flow, in which case one gets simply

$$\mathbf{r}_{i} - \mathbf{r}_{i}^{0} = \mathbf{U}\Delta t + \sum_{j} (\nabla_{j} \cdot \mathbf{D}_{ij}^{0}) \Delta t + \frac{1}{k_{\mathrm{B}}T} \sum_{j} \mathbf{D}_{ij}^{0} \cdot \mathbf{F}_{j}^{0} \Delta t + \mathbf{B}_{i},$$
 (5)

where U is the flow velocity. If the diffusion tensor is nondiagonal, there exists a coupling between the force acting on the particle j and the displacement of particle i (cf equation (3)). This coupling, mediated by the solvent, is commonly referred to as the 'hydrodynamic interactions'.

Note that without the HI the diffusion tensor is simply

$$\mathbf{D}_{ij} = \frac{k_{\rm B}T}{\nu} \mathbf{I} \delta_{ij} \tag{6}$$

and we recover the overdamped limit of equation (1). The diffusion tensor **D** depends in a complicated nonlinear way on the instantaneous positions of all particles in the system. For a system of spheres, exact explicit expressions for the diffusion tensor \mathbf{D}_{ij} exist in the form of the power series in interparticle distances, which may be incorporated into the simulation scheme [31–37]. Here we adopt a pairwise, far-field approximation of **D** proposed by Rotne, Prager [38] and Yamakawa [39],

$$\mathbf{D}_{ii} = \frac{k_{\mathrm{B}}T}{\gamma}\mathbf{I} \tag{7}$$

and

$$\mathbf{D}_{ij} = \frac{k_{\rm B}T}{\gamma} \frac{3a}{4r_{ij}} \left\{ \begin{bmatrix} \left(1 + \frac{2a^2}{3r_{ij}^2} \right) \mathbf{I} + \left(1 - \frac{2a^2}{r_{ij}^2} \right) \hat{\mathbf{r}}_{ij} \hat{\mathbf{r}}_{ij} \end{bmatrix}, \qquad r_{ij} \geqslant 2a \\ \frac{r_{ij}}{2a} \left[\left(\frac{8}{3} - \frac{3r_{ij}}{4a} \right) \mathbf{I} + \frac{r_{ij}}{4a} \hat{\mathbf{r}}_{ij} \hat{\mathbf{r}}_{ij} \right], \qquad r_{ij} < 2a \end{cases}$$
(8)

where $\mathbf{r}_{ij} = \mathbf{r}_j - \mathbf{r}_i$ and a represents the hydrodynamic radius of a bead. Since the above expression is exact only in the large- r_{ij} limit, the radius a should be taken to be significantly smaller than 1.9 Å, which is half of the distance between the successive beads. On the other hand, a cannot be too small, since the space along the chain is densely filled with amino-acids. We take a = 1.5 Å in our simulations, which seems to be a reasonable starting point for a qualitative assessment of HI impact on protein unfolding. However, further studies on the impact of a on the system dynamics are needed; in particular, the hydrodynamic radius might need to vary along the chain, reflecting the different sizes of residues.

In the approximation (8), the divergence of the diffusion matrix vanishes $(\nabla_j \cdot \mathbf{D}_{ij} \equiv 0)$, which further simplifies the numerical scheme. However, if the full hydrodynamic interactions are included, the divergence term should be taken into account [40].

The simulation using equation (3) together with (7) and (8) will be referred to as Brownian dynamics with hydrodynamic interactions (BDHI), in contrast to a simple BD with the diagonal diffusion tensor (6).

Note that the BD describes configurational evolution of the beads on timescales in which the inertia effects of the beads and solvent molecules are negligible [41] and, therefore, timescale separation issues discussed in section 3 are not pertinent here. This feature favours

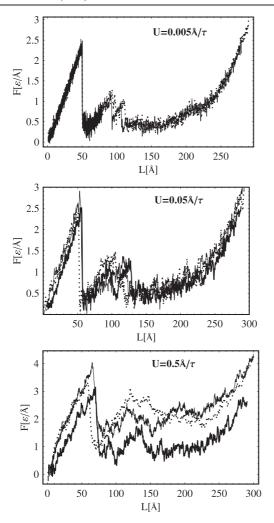


Figure 1. Force–extension curves for the ubiquitin unfolding at a constant speed obtained using Langevin dynamics (dotted line) and Brownian dynamics with (thick solid line) and without (thin solid line) hydrodynamic interactions. The successive panels correspond to the pulling speeds of $v_p = 0.5, 0.05$ and $0.005 \text{ Å}/\tau$ from bottom to top respectively.

BD as a method of choice when simulating stochastically driven motion of proteins at a coarse-grained level [4].

In our previous studies on ubiquitin unfolding [16, 42], we have used LD. Here, on the other hand, we incorporate HI within the BD approach. This calls for a comparison of the three schemes (LD, BD, and BDHI) to distinguish the effects resulting from HI and those from the usage of distinct integration schemes.

5. Constant-velocity stretching

Figure 1 presents the force–extension curves for the constant-velocity unfolding at different unfolding speeds. In the simulations, both termini of a protein are attached to harmonic springs with the elastic constant $k = 0.06\epsilon \text{ Å}^{-2}$. The other end of the N-terminus spring is fixed

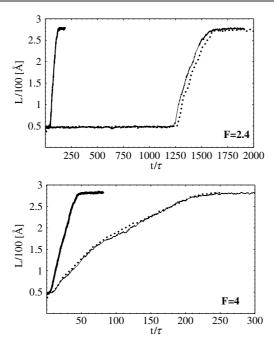


Figure 2. The end-to-end distance of the model ubiquitin as a function of time during unfolding at a constant force. The thick solid, thin solid, and dotted lines correspond to the BDHI, BD and LD simulations respectively. The upper panel corresponds to the force $F=2.4\epsilon~\text{Å}^{-1}$, and the lower one to $F=4\epsilon~\text{Å}^{-1}$.

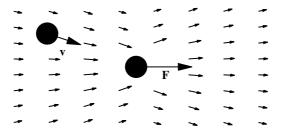


Figure 3. The dragging effect: the moving particle creates a flow pattern which affects other particles by pulling them in the direction of its motion.

whereas the C-terminus spring moves at a speed v_p . We consider three values of v_p : 0.5, 0.05 and $v_p = 0.005 \text{ Å}/\tau$.

In the low-speed limit, all the three data sets obtained using the LD, BD and BDHI are seen to converge to a single curve. In contrast, at large unfolding speeds, the differences between the LD and BD are pronounced. However, strictly speaking, in this time regime BD has a limited validity, because of the lack of separation between the momentum relaxation time $(t_v = \frac{m}{\gamma} = 0.5\tau)$ and the characteristic time of the amino-acid movement due to the stretching $t_{\text{pull}} = \frac{a}{v_{\text{p}}} = 3\tau$ (for the highest speed quoted above). In the experiments, the separation of timescales is huge. In water $\gamma \approx 6\pi \eta a \approx 3 \times 10^{-9} \text{ g s}^{-1}$, which leads to $\tau_v = \frac{m}{\gamma} \approx 0.06 \text{ ps}$ (for the typical amino-acid mass of $m \approx 2 \times 10^{-22} \text{ g}$). On the other hand, the pulling speeds are of the order of 500 nm s⁻¹, which gives $\tau_p \approx 0.3$ ms, thus there is a five-order-of-magnitude

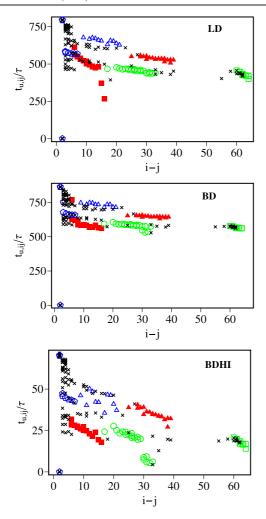


Figure 4. Unfolding scenarios of ubiquitin at constant force of $F=2.4\epsilon$ Å⁻¹ simulated with LD (the upper panel), BD (the centre panel), and BDHI (the lower panel). Open circles, triangles, squares, pentagons and solid triangles and squares correspond to contacts (38–50)–(65–72), (12–17)–(23–34), [(1–7), (12–17)]–(65, 72), (41–49)–(41–49), (17–27)–(51–59), and (1–7)–(12–17) respectively. The crosses denote all other contacts. The segment (23–34) corresponds to a helix. The two β-strands (1–7) and (12–17) form a hairpin. The remaining β-strands are (17–27), (41–49), and (51–59).

separation in timescales. For such a case, LD and BD simulations would give exactly the same result.

The fact that the differences between the BD and BDHI trajectories disappear in the limit of small v_p is due to the lack of impact of HI at small velocities. To conclude, in the experimentally relevant small-speed limit, the effects of HI are expected to be negligible.

An inspection of figure 1 indicates that in the case of high stretching speeds neglecting HI results in larger peak forces. In the high-speed all-atom simulations of titin in water [21] the forces of stretching are found to be excessively large. Such all-atom molecular dynamics programs are not geared towards hydrodynamic phenomena and may incorporate HI poorly. It is possible to consider that the excessive force could be partially due to the missing HI.

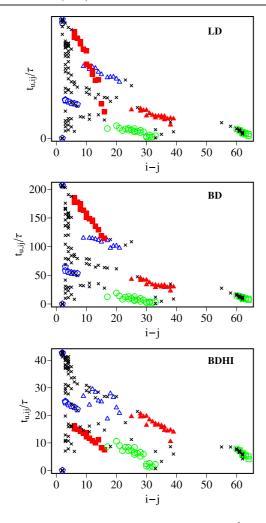


Figure 5. The same as in figure 3 but for $F = 4\epsilon \text{ Å}^{-1}$.

6. Force-clamp unfolding

In the force-clamp AFM unfolding [10, 11] one applies the stretching force to the protein terminus and monitors the end-to-end distance, L. The experimental data and the numerical simulations [16, 17] show that proteins unfold in a stepwise manner at a constant force. This means that a rapid unfolding transition takes place after a certain waiting time. The smaller the force, the longer the waiting time.

In our simulations, we apply the force to the C terminus of the protein, whereas the N-terminus is attached to a harmonic spring of elastic constant $k=0.06\epsilon$ Å $^{-2}$. The unfolding trajectories of ubiquitin are presented in figure 2 for two values of the force, $F=2.4\epsilon$ Å $^{-1}$ and $F=4\epsilon$ Å $^{-1}$. The LD and BD methods essentially coincide for these relatively large forces (small differences between the trajectories are merely stochastic in nature). However, the inclusion of HI changes the physics considerably—the waiting times become much smaller and the duration of the unfolding transition itself decreases from $\approx 250\tau$ to about 50τ at both values of the force.

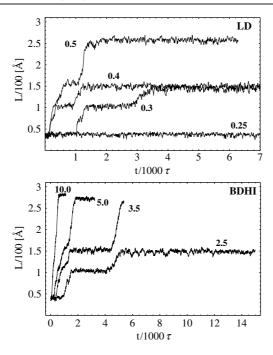


Figure 6. The end-to-end distance of the model ubiquitin as a function of time during unfolding by a uniform fluid flow as illustrated by several trajectories. The lower panel corresponds to the description with the hydrodynamic interactions and the upper without. The successive curves in the upper panel correspond to the flows of 0.25, 0.3, 0.4 and 0.5 Å/ τ from bottom to top respectively. In the lower panel the flow speeds are 2.5, 3.5, 5.0, and 10.0 Å/ τ In all the simulations, the N-terminus of the protein is fixed.

The fact that the HI facilitate protein unfolding may be understood qualitatively when one realizes that an amino-acid moving away from the bulk of a protein creates a flow which drags other residues with it (see figure 3).

The differences between unfolding with and without HI are further highlighted by analysis of the so-called unfolding scenarios [25], in which one plots an average time when a given contact is broken against the contact order, i.e. against the sequential distance, |j-i|, between the amino-acids that form a native contact. Figures 4 and 5 compare the unfolding scenarios for LD, BD, and BDHI at $F=2.4\epsilon$ Å⁻¹ and $F=4\epsilon$ Å⁻¹ respectively. Remarkably, although the differences in timescales between the unfolding with and without HI are considerable, the unfolding scenarios for the smaller force are similar (figure 4), which shows that the unfolding pathway of a protein is not affected by the hydrodynamic effects. However, as the force is increased, both LD and BD scenarios change (figure 5): the β -hairpin structure now unfolds at the end instead of at the beginning of the unfolding process. In contrast, in the case of BDHI, such a switch is not observed: the scenarios for larger and smaller forces look qualitatively similar.

7. Unfolding in a uniform flow

Finally, we study the influence of HI on the characteristics of the protein unfolding in a uniform flow with a speed of U. Although the process has not yet been realized experimentally,

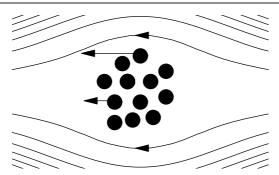


Figure 7. The shielding effect: the particles inside a cluster experience a smaller drag force than those on the surface

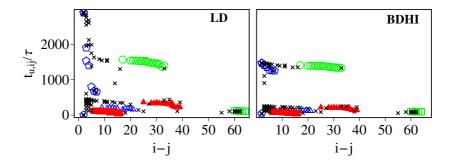


Figure 8. The left and right panels show unfolding scenarios without the hydrodynamic interactions $(U = 0.55 \text{ Å}/\tau)$ and with the hydrodynamic interactions $(U = 3.5 \text{ Å}/\tau)$ respectively.

the simulations [42–44] seem to suggest that uniform flow unfolding leads to a richer set of metastable conformations than the constant force pulling. For example, when the N terminus is anchored, ubiquitin stretches in a flow through two distinct intermediate states corresponding to a partial unzipping.

A detailed analysis of the uniform flow unfolding of ubiquitin in the absence of HI, together with the snapshots of intermediate conformations for different anchorings, can be found in [42]. In that reference, we have mistakenly reported values of the forces in wrong units. Instead of the correct unit of $\epsilon/\text{Å}$ we used ϵ/σ , where σ was equal to 5 Å.

Figure 6 shows examples of unfolding trajectories of ubiquitin in a uniform flow for four different flow velocities, both with and without HI. We observe that unfolding of the system with HI requires a much larger flow speed than without. This can be understood qualitatively in terms of the so-called no-draining effect [45]: the residues hidden inside the protein are shielded from the flow and thus only a small fraction of the residues experience the full drag force of $F = -\gamma U$ (see figure 7). In contrast, when no HI are present, this drag force is applied to all residues [42].

Notably, although the timescales and velocities involved in the protein unfolding with and without HI are completely different, the metastable states are nearly identical (see figure 6). This feature is related to the dynamic character of HI—they do not change the potential energy of the system and, therefore, do not affect its stationary properties. In principle, however, one could imagine a situation in which, due to the differences in dynamics imposed by HI, a system chooses alternative pathways when unfolding. This is clearly not the case here, which may be

related to the *directed* character of the disturbance (flow in this case or the force in a forceclamp experiment), which imposes a preferred direction of unfolding, thus greatly reducing the set of available unfolding pathways.

The similarities in unfolding pathways of ubiquitin are further confirmed by the comparison of unfolding scenarios. As an example, figure 8 shows the unfolding scenario for the flow $U=3.5~\text{Å}/\tau$ with HI compared to $U=0.55~\text{Å}/\tau$ without HI (the mean unfolding times are comparable in both cases). The scenarios are very close to each other, the main difference being that the HI enhance cooperativity by breaking the contacts in a more simultaneous fashion.

8. Summary

In summary, hydrodynamic interactions seem to affect the timescales of unfolding by a constant force and by a fluid flow in opposite ways but keep the set of the possible metastable states. The HI may also reduce peak forces in stretching at a constant speed, although this effect weakens with the diminishing stretching speed.

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